

### Wende eine Binomische Formel an:

$$(x + 2y)^2 = x^2 + 4xy + 4y^2$$

$$(3x - y)^2 = 9x^2 - 6xy + y^2$$

$$(a + 4b)(a - 4b) = a^2 - 16b^2$$

$$(2a - 3b)^2 = 4a^2 - 12ab + 9b^2$$

$$(5x + 2y)^2 = 25x^2 + 20xy + 4y^2$$

$$(3x + 2y)(3x - 2y) = 9x^2 - 4y^2$$

$$(x^2 - y^2)^2 = x^4 - 2x^2y^2 + y^4$$

$$(2x^3 + 3y^2)^2 = 4x^6 + 12x^3y^2 + 9y^4$$

### Wende die Formeln nun umgekehrt an:

$$x^2 + 2xy + y^2 = (x + y)^2$$

$$4a^2 - 12ab + 9b^2 = (2a - 3b)^2$$

$$4u^2 - 16v^2 = (2u - 4v)(2u + 4v)$$

$$64x^2 + 16xy + y^2 = (8x + y)^2$$

$$a^4 - b^6 = (a^2 + b^3)(a^2 - b^3)$$

$$81x^4 + 36x^2y + 4y^2 = (9x^2 + 2y)^2$$

$$4x^4y^4 - 36a^2 = (2x^2y^2 + 6a)(2x^2y^2 - 6a)$$

$$x^8 + 8x^4 + 16 = (x^4 + 4)^2$$

$$(x - xy)^2 - a^4 = (x - xy + a^2)(x - xy - a^2)$$

### Löse die Klammern soweit wie möglich auf:

$$(2a + 3b)^2 = 4a^2 + 12ab + 9b^2$$

$$(a - 5b^2)^2 = a^2 - 10ab^2 + 25b^4$$

$$(2a - 3b)(2a + 3b) = 4a^2 - 9b^2 \quad (3. \text{ Bin. Formel})$$

$$(3ab + 2bc)^2 = 9a^2b^2 + 12ab^2c + 4b^2c^2$$

$$(a - b)^2 - (a + b)^2 = a^2 - 2ab + b^2 - a^2 - 2ab - b^2 = -4ab$$

### Faktorisiere soweit wie möglich:

$$9ab^2 - 4ac^2 = a(9b^2 - 4c^2) = a(3b + 2c)(3b - 2c)$$

$$a^2 - 16ab + 64b^2 = (a - 8b)^2$$

$$2a^2 + 4ab + 2b^2 = 2(a^2 + 2ab + b^2) = 2(a + b)^2$$

$$a^2b - bc^2 = b(a^2 - c^2) = b(a + c)(a - c)$$

$$2a^2 + 6\sqrt{2}ab + 9b^2 = (\sqrt{2}a + 3b)^2$$

$$12a^2 - 27b^2 = 3(4a^2 - 9b^2) = 3(2a + 3b)(2a - 3b)$$

$$9a^4 + 12a^2b^2 + 4b^4 = (3a^2 + 2b^2)^2$$

$$ab - abc^2 = ab(1 - c^2) = ab(1 + c)(1 - c)$$

$$a + 4ab + 4ab^2 = a(1 + 4b + 4b^2) = a(1 + 2b)^2$$